$\qquad$ Name: $\qquad$
Absent:

## IEEE 754 Standard Floating Point Representation

## 8-bit

|  | Sign <br> bit |
| :--- | :--- |
| Exponent <br> (bias 127) | 23-bit Mantissa <br> (for normalized values, leading 1 not stored) |
| $0 \equiv+\square$ |  |
| $1 \equiv-\square$ |  |

11-bit
Sign Exponent
52-bit Mantissa


| Single Precision |  | Double Precision |  | Object |
| :---: | :---: | :---: | :---: | :---: |
| Exponent | Mantissa | Exponent | Mantissa | Represented |
| $1-254$ | any value | $1-2046$ | any value | normalized \# |
| 0 | 0 | 0 | 0 | 0 |
| 0 | nonzero | 0 | nonzero | denormalized \# |
| 255 | 0 | 2,047 | 0 | infinity |
| 255 | nonzero | 2,047 | nonzero | NaN (not a \#) |

1) Convert the value $23.625_{10}$ to its binary representation.

2) Normalize the above value so that the most significant 1 is immediately to the left of the radix point. Include the corresponding exponent value to indicate the motion of the radix point.

3) Write the corresponding 32-bit IEEE 754 floating point representation for $23.625_{10}$.
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4) Write the corresponding 64-bit IEEE 754 floating point representation for $23.625_{10}$.
5) What would be the smallest positive normalized 32-bit IEEE 754 floating point value?
6) The smallest positive denormalized 32-bit IEEE 754 floating point value has representation of 8-bit

|  | Sign bit | Exponent <br> (bias 127) | 23-bit Mantissa <br> (for denormalized values, leading 0 not stored) |  |
| :---: | :---: | :---: | :---: | :---: |
| $0 \equiv+$ | 0 | 00000000 | $000 \ldots$ | 01 |

What value would it represent?

$$
2 \square_{\times 2} \square
$$

7) What would be the representation for the largest positive denormalized 32-bit IEEE 754 floating point?

|  |  | 8-bit Exponent (bias 127) | 23-bit Mantissa (for denormalized values, leading 0 not stored) |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & 0 \equiv+ \\ & 1 \equiv- \end{aligned}$ | 0 | 0000000 |  |

8) How would you add two IEEE 754 floating point numbers?
9) How would you multiply two IEEE 754 floating point numbers?
10) Consider adding $1.011 \times 2^{40}$ and $1.01 \times 2^{5}$.
a) How many places does the second number's mantissa get shifted?
b) After we add these two numbers and store the results back into a 32-bit IEEE 754 value, what would be the result?
