1. Sum the following binary (base 2) numbers

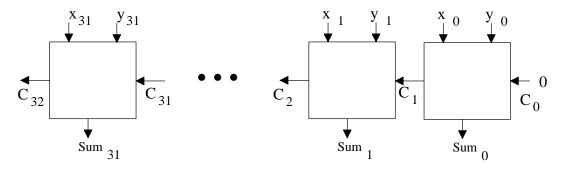
101101<sub>2</sub> +110111<sub>2</sub>

2. Complete the Full-Adder truth table for the sum  $(s_i)$  and carry-out  $(c_{i+1})$  functions.

1		carry-in	sum	carry-out c <sub>i+1</sub>
$\mathbf{X_{i}}$	$\mathbf{y_i}$	$\mathbf{c_i}$	$\mathbf{S_{i}}$	$\mathbf{c}_{i+1}$
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

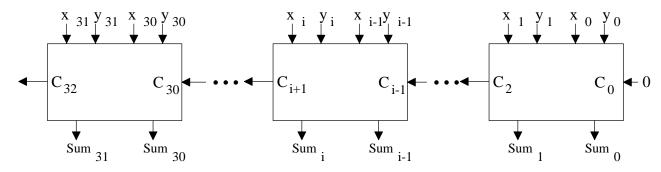
3. Use k-maps to minimize the sum  $(s_i)$  and carry-out  $(c_{i+1})$  functions of the Full-Adder:

- 4. For the one-bit Full-Adder, how many gate delays are needed before the carry-out  $(c_{i+1})$  wire is correct?
- 5. A 32-bit, ripple-adder is made up of a collection of single-bit Full-Adders connected together as shown below:



How many gate delays are needed before  $c_{32}$  is correct?

6. To speed up the calculation of the carry-out  $(C_{i+1})$  signals, consider constructing a 32-bit adder using two-bit adders as shown in:



If  $c_{i+1}$  is calculated directly from the inputs as  $c_{i+1} = x_i y_i + x_i x_{i-1} y_{i-1} + x_i x_{i-1} c_{i-1} + x_i y_{i-1} c_{i-1} + x_i y_{i-1} c_{i-1} + y_i x_{i-1} c_{i-1} + y_i y_{i-1} c_{i-1}$ , then how many gate delays would be needed to calculate the  $c_{i+1}$  signal in a two-bit adder?

- 7. What would be the total number of gate delays in a 32-bit adder before the  $c_{32}$  signal is generated correctly if **two-bit adders** were used?
- 8. What would be the total number of gate delays in a 32-bit adder before the  $c_{32}$  signal is generated correctly if **three-bit adders** were used (10 three-bit adders and a 2-bit adder)?

9. What would be the total number of gate delays in a 32-bit adder before the  $c_{32}$  signal is generated correctly if **four-bit adders** were used?