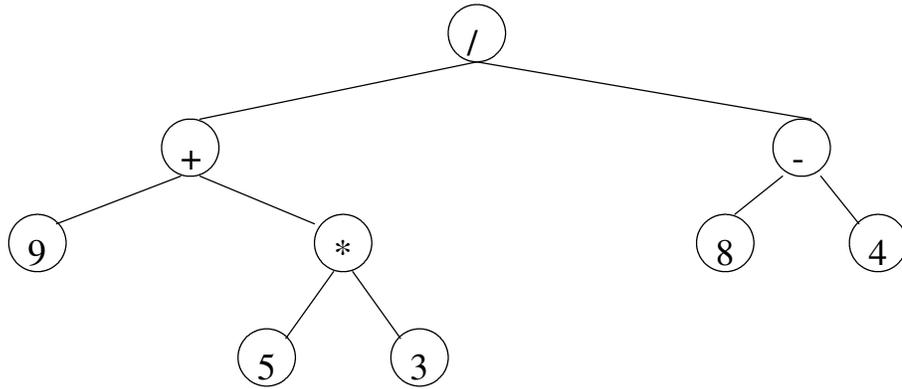


Team #: _____
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Name: _____

0. Consider the parse tree for $(9 + (5 * 3)) / (8 - 4)$:



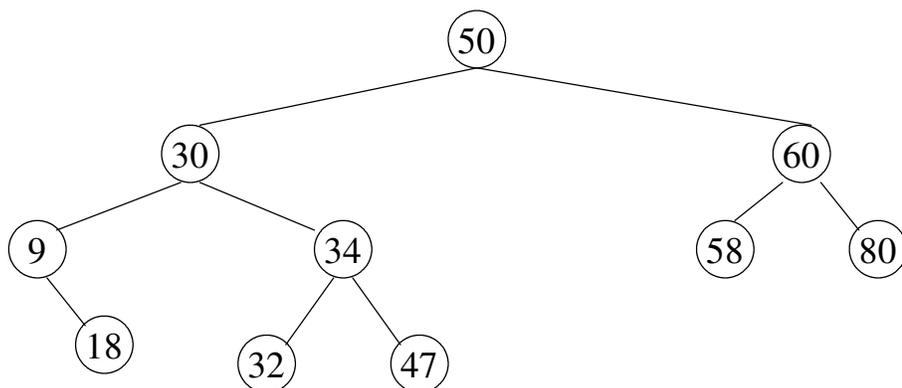
Identify the following items in the above tree:

- node containing “*”
- edge from node containing “-” to node containing “8”
- root node
- children of the node containing “+”
- parent of the node containing “3”
- siblings of the node containing “*”
- leaf nodes of the tree
- subtree whose root is node contains “+”
- path from node containing “+” to node containing “5”
- branch from root node to “3”
- mark the *levels* of the tree (level is the number of edges on the path from the root)
- What is the *height* (max. level) of the tree?

Team #: _____
Absent: _____

Name: _____

1. Consider the Binary Search Tree (BST):



- What would be the result of an inorder traversal?
 - Starting at the root, how would you find the node containing “32”?
 - Starting at the root, when would you discover that “70” is not in the BST?
 - Starting at the root, where would be the “easiest” place to add “70”?
2. a) If a BST contains n nodes and we start searching at the root, what would be the worst-case theta $\Theta()$ notation for a successful search? (Draw the shape of the BST leading to the worst-case search)

b) We could store a BST in an array like we did for a binary heap, what would be the worst-case storage needed for a BST with n nodes?

3. a) If a BST contains n nodes, draw the shape of the BST leading to best, successful search in the worst case.

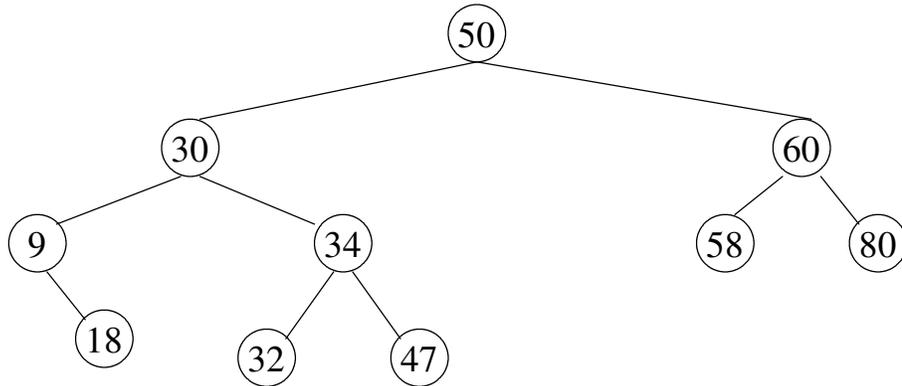
b) What is the worst-case theta $\Theta()$ notation for a successful search in this “best” shape BST?

Team #: _____

Name: _____

Absent:

4. Consider the Binary Search Tree (BST):



- What would be the result of deleting 58 from the BST?
- What would be the result of deleting 9 from the BST?
- What would be the result of deleting 50 from the BST? (Hint: One technique when programming is to convert a hard problem into a simpler problem. Deleting a BST node that contains two children is a hard problem. Since we know how to delete a BST node with none or one child, how could we convert “deleting a node with two children” problem into a simpler problem?)

Absent:

```
//Specification file for the IntBinaryTree class
#ifndef INTBINARYTREE_H
#define INTBINARYTREE_H

class IntBinaryTree {
private:
    struct TreeNode {
        int value;           // The value in the node
        TreeNode *left;     // Pointer to left child node
        TreeNode *right;    // Pointer to right child node
    };

    TreeNode *root;        // Pointer to the root node

    // Private member functions
    void insert(TreeNode *&, TreeNode *&);
    void destroySubTree(TreeNode *);
    void deleteNode(int, TreeNode *&);
    void makeDeletion(TreeNode *&);
    void displayInOrder(TreeNode *) const;
    void displayPreOrder(TreeNode *) const;
    void displayPostOrder(TreeNode *) const;

public:
    // Constructor
    IntBinaryTree()
        { root = NULL; }

    // Destructor
    ~IntBinaryTree()
        { destroySubTree(root); }

    // Binary tree operations
    void insertNode(int);
    bool searchNode(int);
    void remove(int);

    void displayInOrder() const
        { displayInOrder(root); }

    void displayPreOrder() const
        { displayPreOrder(root); }

    void displayPostOrder() const
        { displayPostOrder(root); }
};
#endif
```