- 4.11 Consider a memory system that uses a 32-bit address to address at the byte level, plus a cache that uses a 64-byte line size.
  - a. Assume a direct mapped cache with a tag field in the address of 20 bits. Show the address format and determine the following parameters: number of addressable units, number of blocks in main memory, number of lines in cache, size of tag.
  - b. Assume an associative cache. Show the address format and determine the following parameters: number of addressable units, number of blocks in main memory, number of lines in cache, size of tag.
  - c. Assume a four-way set-associative cache with a tag field in the address of 9 bits. Show the address format and determine the following parameters: number of addressable units, number of blocks in main memory, number of lines in set, number of sets in cache, number of lines in cache, size of tag.
- 4.18 Consider a cache of 4 lines of 16 bytes each. Main memory is divided into blocks of 16 bytes each. That is, block 0 has bytes with addresses 0 through 15, and so on. Now consider a program that accesses memory in the following sequence of addresses:

  Once: 63 through 70

Loop ten times: 15 through 32; 80 through 95

- a. Suppose the cache is organized as direct mapped. Memory blocks 0, 4, and so on are assigned to line 1; blocks 1, 5, and so on to line 2; and so on. Compute the hit ratio.
- b. Suppose the cache is organized as two-way set associative, with two sets of two lines each. Even-numbered blocks are assigned to set 0 and odd-numbered blocks are assigned to set 1. Compute the hit ratio for the two-way set-associative cache using the least recently used replacement scheme.
- 4.21 Consider a single-level cache with an access time of 2.5 ns, a line size of 64 bytes, and a hit ratio of H = 0.95. Main memory uses a block transfer capability that has a firstword (4 bytes) access time of 50 ns and an access time of 5 ns for each word thereafter.
  - a. What is the access time when there is a cache miss? Assume that the cache waits until the line has been fetched from main memory and then re-executes for a hit.
  - b. Suppose that increasing the line size to 128 bytes increases the H to 0.97. Does this reduce the average memory access time?