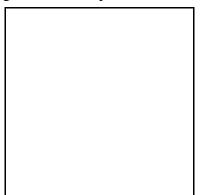
Data Structures - Test 2

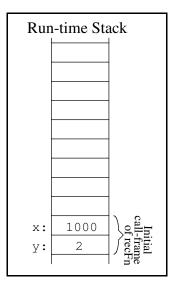
Question 1. (5 points) What is printed by the following program?

```
def recFn(x, y):
    print( x, y )
    if x <= y:
        return x
    else:
        return x + recFn(x // 10, y + 1) + y

print("Result = ", recFn(1000, 2))</pre>
```



Output:



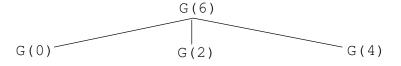
Question 2. (8 points) Write a recursive Python function to compute the following mathematical function, G(n):

G(n) = n for all value of $n \le 0$

G(n) = G(n-6) + G(n-4) + G(n-2) for all values of n > 0.

def G(n):

Question 3. (7 points) a) For the above recursive function G(n), complete the calling-tree for G(6).



- b) What is the value of G(6)?
- c) What is the maximum height of the run-time stack when calculating G(6) recursively?

Question 4. (15 points.) Consider the following insertion sort code which sorts in ascending order.

```
def insertionSort(myList):
    for firstUnsortedIndex in range(1,len(myList)):
        itemToInsert = myList[firstUnsortedIndex]
        testIndex = firstUnsortedIndex - 1

    while testIndex >= 0 and myList[testIndex] > itemToInsert:
        myList[testIndex+1] = myList[testIndex]
        testIndex = testIndex - 1

    myList[testIndex + 1] = itemToInsert
```

- a) What is the purpose of the testIndex >= 0 while-loop comparison?
- b) Consider the modified insertion sort code that eliminates the testIndex >= 0 while-loop comparison.

```
def insertionSortB(myList):
    minIndex = 0
    for testIndex in range(1,len(myList)):
        if myList[testIndex] < myList[minIndex]:
            minIndex = testIndex
    temp = myList[0]
    myList[0] = myList[minIndex]
    myList[minIndex] = temp

for firstUnsortedIndex in range(1,len(myList)):
    itemToInsert = myList[firstUnsortedIndex]
    testIndex = firstUnsortedIndex - 1

    while myList[testIndex] > itemToInsert:
        myList[testIndex+1] = myList[testIndex]
        testIndex = testIndex - 1

    myList[testIndex + 1] = itemToInsert
```

b) Explain how the bolded code in the modified insertion sort code above allows for the elimination of the testIndex >= 0 while-loop comparison.

Consider the following timing of the above two insertion sorts on lists of 10000 elements.

Initial arrangement of list before sorting	insertionSort - at the top of page	insertionSortB - modified version in middle of the page
Sorted in descending order: 10000, 9999,, 2, 1	14.0 seconds	12.3 seconds
Already in ascending order: 1, 2,, 9999, 10000	0.005 seconds	0.004 seconds
Randomly ordered list of 10000 numbers	7.3 seconds	6.4 seconds

- c) Explain why insertionSortB (modified version in middle of page) out performs the original insertionSort.
- d) In either version, why does sorting the randomly order list take about halve the time of sorting the initially descending ordered list?

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Question 5. (20 points) Write a variation of selection sort that:

- sorts in ascending order (smallest to largest)
- builds the sorted part on the left-hand side of the list, i.e.,

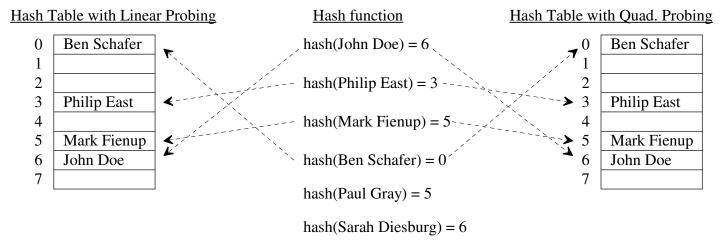
Sorted Part	Unsorted Part

def selectionSort(myList):

Question 6. (15 points) Recall the common rehashing strategies we discussed for open-address hashing:

Strategy	Description
linear probing	Check next spot (counting circularly) for the first available slot, i.e., (home address + (rehash attempt #)) % (hash table size)
quadratic probing	Check the square of the attempt-number away for an available slot, i.e., [home address + $($ (rehash attempt #) 2 +(rehash attempt #) $)/2$] % (hash table size), where the hash table size is a power of 2. Integer division is used above

a) Insert "Paul Gray" and then "Sarah Diesburg" using Linear (on left) and Quadratic (on right) probing.



b) Explain how deletions in an open-address hash table are handled.

Question 7. (15 points) The general idea of *Quick sort* is as follows:

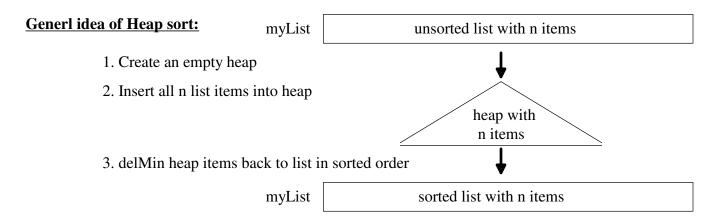
- Select a "random" item in the unsorted part as the *pivot*
- Rearrange (partitioning) the unsorted items such that:
- Quick sort the unsorted part to the left of the pivot
- Quick sort the unsorted part to the right of the pivot

Pivot Index

All items < to Pivot | Pivot | All items >= to Pivot |

Explain why the **best-case** performance is $O(n \log_2 n)$.

Question 8. (15 points) Recall the general idea of Heap sort which uses a min-heap (class BinHeap) to sort a list. (BinHeap methods: BinHeap(), insert(item), delMin(), isEmpty(), size())



- a) If we insert all of the list elements into a min-heap, what item would we easily be able to determine?
- b) Complete the code for heapsort so that it sorts in descending order

```
from bin_heap import BinHeap
def heapSort(myList):
    # Create an empty heap
    myHeap = BinHeap()
```

c) Determine the overall O() for heap sort and justify your answer.