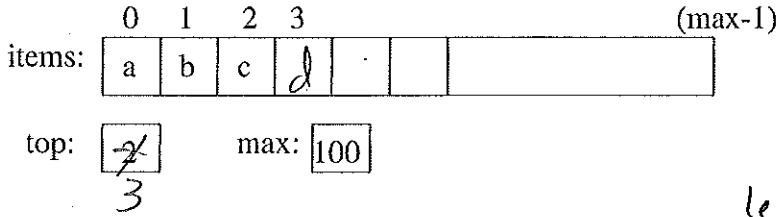


1. An "abstract" view of the stack:

Using an array implementation would look something like:



$n \equiv \# \text{ items in stack}$

Complete the big-oh notation for the following stack methods assuming an array implementation: ("n" is the # items)

	push(item)	pop()	peek()	size()	isEmpty()	isFull()	Constructor
Big-oh	$O(1)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$

2. Since Python does not have a (directly accessible) built-in array, we can use a list.

```

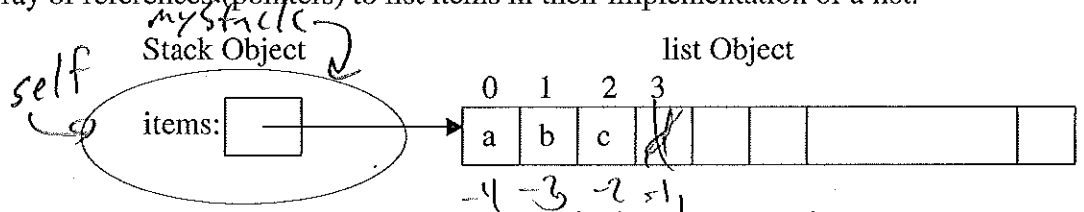
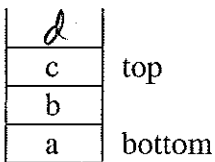
class Stack:
    def __init__(self):
        self.items = []
    def isEmpty(self):
        return self.items == []
    def push(self, item):
        self.items.append(item)
    def pop(self):
        return self.items.pop()
    def peek(self):
        return self.items[len(self.items)-1]
    def size(self):
        return len(self.items)
    
```

*myStack = Stack()*

*return len(self.items) == 0*

Since Python uses an array of references (pointers) to list items in their implementation of a list.

"Abstract" Stack



*when physical size is reached, then  $\sim O(n)$*

a) Complete the big-oh notation for the stack methods assuming this Python list implementation: ("n" is the # items)

	push(item)	pop()	peek()	size()	isEmpty()	<code>__init__</code>
Big-oh	$O(1)^*$	$O(1)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$

b) Which operations should have what preconditions?

*pop - stack is not empty*  
*peek - " " " "*

3. The text's alternative stack implementation also using a Python list is:

```
class Stack:
    def __init__(self):
        self.items = []

    def isEmpty(self):
        return self.items == []

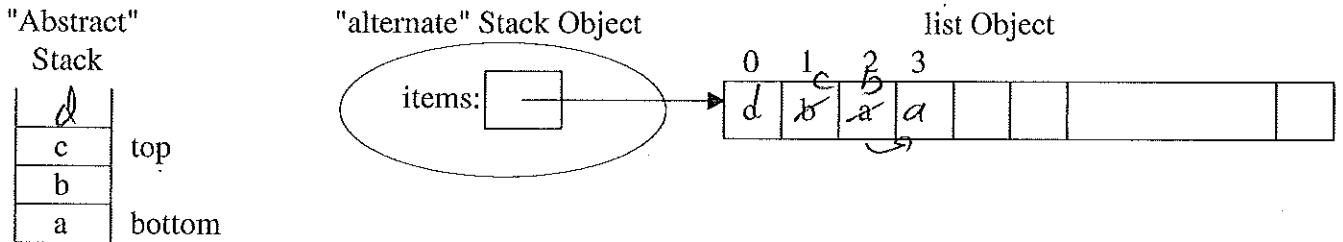
    def push(self, item):
        self.items.insert(0,item)

    def pop(self):
        return self.items.pop(0)

    def peek(self):
        return self.items[0]

    def size(self):
        return len(self.items)
```

Since an array is used to implement a Python list, the alternate Stack implementation using a list:



a) Complete the big-oh notation for the "alternate" Stack methods: ("n" is the # items)

	push(item)	pop()	peek()	size()	isEmpty()	__init__
Big-oh	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(1)$	$O(1)$

4. How could we use a stack to check if a word is a palindrome (e.g. "radar", "toot")?

*Handwritten solution for palindrome check:*

```
def isPalindrome(word):
    n = len(word)
    myStack = Stack()
    for index in range(0, len(word)//2):
        myStack.push(word[index])
    palFlag = True
    for index in range((len(word)+1)//2, len(word)):
        if word[index] != myStack.pop():
            return False # palFlag = False
    return True
return palFlag
```

*Additional notes:*

- A small stack diagram shows 'a' on top and 'v' below it.
- A diagram shows the word "radar" with indices 0, 1, 2, 3, 4 above the letters. An arrow points from index 4 to index 0.
- A diagram shows a list of symbols: [ '(', '(', '(', '(', ']', ']', ']', ']' ] with a checkmark next to it.
- A diagram shows a list of symbols: [ '(', '(', '(', '(', ']', ']', ']', ']' ] with checkmarks next to each element.

5. Scan string from left to right.  
 if opening symbol, then push on stack  
 else if closing symbol, then pop stack and  
 check for matching opening symbol