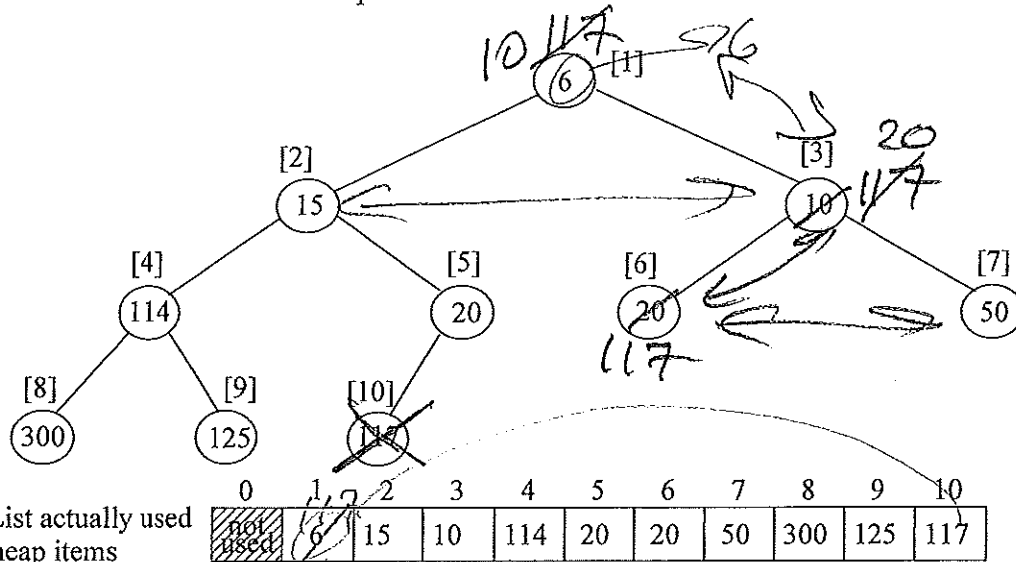




2. Now let us consider the delMin operation that removes and returns the minimum item.



- a) What item would delMin remove and return from the above heap? **6**
- b) What is the quickest way to fill the hole left by delMin? *move right most item to index 1*
- c) What new problem does this cause? *moved item violates heap-order property*

General Idea of delMin():

- remember the minimum value so it can be returned later (easy to find - at index 1)
- copy the last item in the list to the root, delete it from the right end, decrement size
- restore the heap-order property by repeatedly swapping this item with its smallest child until it *percolates* down to the correct spot
- return the minimum value

d) What would the above heap look like after delMin? (show the changes on above tree)

e) Complete the code for the percDown method used by delMin.

<pre> class BinHeap:     def minChild(self, i):         if i * 2 + 1 &gt; self.currentSize: # if only left child             return i * 2         else:             if self.heapList[i * 2] &lt; self.heapList[i * 2 + 1]:                 return i * 2             else:                 return i * 2 + 1      def delMin(self):         retval = self.heapList[1]         self.heapList[1] = self.heapList[self.currentSize]         self.currentSize = self.currentSize - 1         self.heapList.pop()         self.percDown(1)         return retval         </pre>	<pre> def percDown(self, currentIndex):     while True:         if currentIndex * 2 &gt; self.currentSize:             return         minChildIndex = self.minChild(currentIndex)         if self.heapList[currentIndex] &lt; self.heapList[minChildIndex]:             return         temp = self.heapList[currentIndex]         self.heapList[currentIndex] = self.heapList[minChildIndex]         self.heapList[minChildIndex] = temp         currentIndex = minChildIndex         </pre>
--	--

f) What is the big-oh notation for delMin?  **$O(\log n)$**

Once we have a working BinHeap, then implementing the PriorityQueue class using a BinHeap is a piece of cake:

```

### File: priority_queue.py
from binheap import BinHeap

class PriorityQueue:
    def __init__(self):
        self._heap = BinHeap()

    def isEmpty(self):
        return self._heap.isEmpty()

    def enqueue(self, item):
        self._heap.insert(item)

    def dequeue(self):
        return self._heap.delMin()

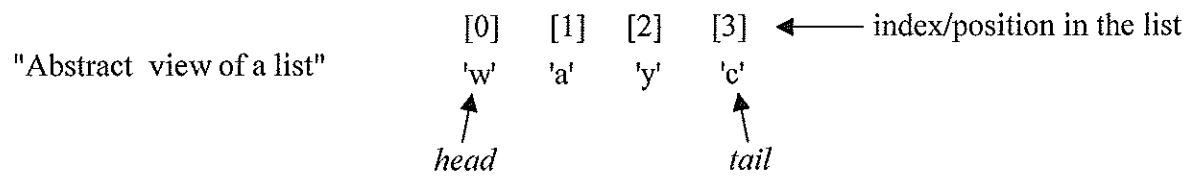
    def size(self):
        return self._heap.size()

    def __str__(self):
        return str(self._heap)
    
```

```

>>> q = PriorityQueue()
>>> print(q)
[]
>>> q.enqueue(5)
>>> q.enqueue(1)
>>> q.enqueue(7)
>>> print(q)
[1, 5, 7]
>>> q.dequeue()
1
>>> print(q)
[5, 7]
    
```

3. A "list" is a generic term for a sequence of items in a linear arrangement. Unlike stacks, queues and dequeues access to list items is not limited to either end, but can be from any position in the list. The general terminology of a list is illustrated by:



There are three broad categories of list operations that are possible:

- **index-based operations** - the list is manipulated by specifying an index location, e.g.,  
`myList.insert(3, item)` # insert item at index 3 in myList
- **content-based operations** - the list is manipulated by specifying some content (i.e., item value), e.g.,  
`myList.remove(item)` # removes the item from the list based on its value
- **cursor-base operations** - a *cursor* (current position) can be moved around the list, and it is used to identify list items to be manipulated, e.g.,  
`myList.first()` # sets the cursor to the head item of the list  
`myList.next()` # moves the cursor one position toward the tail of the list  
`myList.remove()` # deletes the second item in the list because that's where the cursor is currently located

The following table summarizes the operations from the three basic categories on a list, L:

Index-based operations	Content-based operations	cursor-based operations
<code>L.insert(index, item)</code> <code>item = L[index]</code> <code>L[index] = newValue</code> <code>L.pop(index)</code>	<code>L.add(item)</code> <code>L.remove(item)</code> <code>L.search(item)</code> #return Boolean <code>i = L.index(item)</code>	<code>L.hasNext()</code> <code>L.next()</code> <code>L.hasPrevious()</code> <code>L.previous()</code> <code>L.first()</code> <code>L.last()</code> <code>L.insert(item)</code> <code>L.replace(item)</code> <code>L.remove()</code>

Built-in Python lists are unordered with a mixture of index-based and content-based operations. We know they are implemented using a contiguous block of memory (i.e., an array). The textbook talks about an unordered list ADT, and a sorted list ADT which is more content-based. Both are implemented using a singly-linked list.

a) Why would a singly-linked list be a bad choice for implementing a cursor-based list ADT?

```
def percolp(self, currentIndex):  
    parentIndex = currentIndex // 2
```

```
    while parentIndex >= 1 and  
          self.heapList[currentIndex] <  
            self.heapList[parentIndex]:
```

```
        temp = self.heapList[currentIndex]  
        self.heapList[currentIndex] =  
            self.heapList[parentIndex]
```

```
        self.heapList[parentIndex] = temp
```

```
        currentIndex = parentIndex
```

```
        parentIndex = currentIndex // 2
```

```
def percDown (self, currentIndex):
```

```
    while True: leftChildIndex =
```

```
        if  $\text{currentIndex} / 2 > \text{self.currentSize}$ :  
            return
```

```
    else:
```

```
        minChildIndex = self.minChild (self, currentIndex)
```

```
        if self.heapList[currentIndex] <  
            self.heapList[minChildIndex]:
```

```
            temp = self.heapList[currentIndex]
```

```
            self.heapList[currentIndex] = self.heapList  
                [minChildIndex]
```

```
            self.heapList[minChildIndex] = temp
```

```
            currentIndex = minChildIndex
```

```
    else:
```

```
        return
```