Data Structures (CS 1520)

Lecture 27

- 1. There are two general approaches for traversing a graph from some starting vertex *s*:
- Depth First Search (DFS) where you explore as deeply into the graph as possible. If you reach a "dead end," we backtrack to the deepest vertex that allows us to try a different path.
- Breadth First Search (BFS) where you find all vertices a distance 1 (directly connected) from s, before finding all vertices a distance 2 from s, etc.

What data structure would be helpful in each type of search? Why?

a) Breadth First Search (BFS):

b) Depth First Search (DFS):

- 2. On the next page is the textbook's edge, vertex, and graph implementations.
- a) How does this graph implementation maintain its set of vertices?

b) How does this graph implementation maintain its set of edges?

3. Assuming a graph g containing the word-ladder graph from lecture 26, on the diagram trace the bfs algorithm by showing the value of each vertex's color, predecessor, and distance attributes?

""" File: vertex.py """ """ File: graph.py """ from vertex import Vertex class Vertex: def __init__(self, key, color = 'white', dist = 0, pred = None): self.id = key self.connectedTo = {} self.color = color self.predecessor = pred self.distance = dist self.discovery = 0self.finish = 0def addNeighbor(self, nbr, weight=0): self.connectedTo[nbr] = weight def __str_(self): return str(self.id) + ' connectedTo: ' + str([x.id for x in self.connectedTo]) def getConnections(self): return self.connectedTo.keys() def getId(self): return self.id def getWeight(self,nbr): return self.connectedTo[nbr] def getColor(self): return self.color def setColor(self, newColor): self.color = newColor def getPred(self): return self.predecessor def setPred(self, newPred): self.predecessor = newPred def getDiscovery(self): return self.discovery def setDiscovery(self, newDiscovery): self.discovery = newDiscovery def getFinish(self): return self.Finish def setFinish(self, newFinish): self.finish = newFinish def getDistance(self): return self.distance def setDistance(self, newDistance): self.distance = newDistance

class Graph: def __init__(self): self.vertList = {} self.numVertices = 0 def addVertex(self,key): self.numVertices = self.numVertices + 1 newVertex = Vertex(key) self.vertList[key] = newVertex return newVertex def getVertex(self,n): if n in self.vertList: return self.vertList[n] else: return None def __contains__(self,n): return n in self.vertList def addEdge(self,f,t,cost=0): if f not in self.vertList: nv = self.addVertex(f) if t not in self.vertList: nv = self.addVertex(t) self.vertList[f].addNeighbor \ (self.vertList[t], cost) def getVertices(self): return self.vertList.keys() def __iter__(self): return iter(self.vertList.values())

```
""" File: graph_algorithms.py """
from graph import Graph
from vertex import Vertex
from linked_queue import LinkedQueue
def bfs(g,start):
 start.setDistance(0)
 start.setPred(None)
 vertQueue = LinkedQueue()
 vertQueue.enqueue(start)
 while (vertQueue.size() > 0):
    currentVert = vertQueue.dequeue()
    for nbr in currentVert.getConnections():
     if (nbr.getColor() == 'white'):
       nbr.setColor('gray')
       nbr.setDistance(currentVert.getDistance()+1)
       nbr.setPred(currentVert)
       vertQueue.enqueue(nbr)
    currentVert.setColor('black')
```

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4. Section 7.5 uses recursion and the run-time stack to implement a DFS traversal. The DFSGraph uses a time attribute to note when a vertex if first encountered (discovery attribute) in the depth-first search and when a vertex in backtracked through (finish attribute). Consider the graph for making pancakes where vertices are steps and edges represents the partial order among the steps.



from graph import Graph class DFSGraph(Graph):	
def	<pre>init(self): super()init() self.time = 0</pre>
def	<pre>dfs(self): for aVertex in self: aVertex.setColor('white') aVertex.setPred(-1) for aVertex in self: if aVertex.getColor() == 'white': self.dfsvisit(aVertex)</pre>
def	<pre>dfsvisit(self,startVertex): startVertex.setColor('gray') self.time += 1 startVertex.setDiscovery(self.time) for nextVertex in startVertex.getConnections(): if nextVertex.getColor() == 'white': nextVertex.setPred(startVertex) self.dfsvisit(nextVertex) self.dfsvisit(nextVertex) startVertex.setColor('black') self.time += 1 startVertex.setFinish(self.time)</pre>

a) Assume (why is this a bad assumption???) that the for-loops alway iterate through the vertexes alphabetically (e.g., "eat", "egg", "flour", ...) by their id. Write on the above graph the discovery and finish attributes assigned to each vertex by executing the dfs method?

b) A *topological sort* algorithm can use the dfs discovery and finish attributes to determine a proper order to avoid putting the "cart before the horse." For example, we don't want to "pour ½ cup of batter" before we "mix the batter", and we don't want to "mix the batter" until all the ingredients have been added. Outline the steps to perform a topological sort.

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5. Consider the following directed graph (diagraph).



Dijkstra's Algorithm is a *greedy algorithm* that finds the shortest path from some vertex, say v_0 , to all other vertices. A *greedy algorithm*, unlike divide-and-conquer and dynamic programming algorithms, DOES NOT divide a problem into smaller subproblems. Instead a greedy algorithm builds a solution by making a sequence of choices that look best ("locally" optimal) at the moment without regard for past or future choices (no backtracking to fix bad choices). Dijkstra's algorithm builds a subgraph by repeatedly selecting the next closest vertex to v_0 that is not already in the subgraph. Initially, only vertex v_0 is in the subgraph with a distance of 0 from itself.

a) What would be the order of vertices added to the subgraph during Dijkstra's algorithm? v_0 ,

b) What greedy criteria did you use to select the next vertex to add to the subgraph?

c) What data structure could be used to efficiently determine that selection?

d) How might this data structure need to be modified?