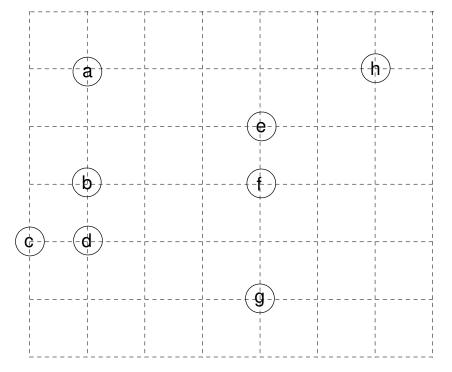
Lecture 28

1. Suppose you had a map of settlements on the planet X (Assume edges could connecting all vertices with their Euclidean distances as their costs)



We want to build roads that allow us to travel between any pair of cities. Because resources are scarce, we want the total length of all roads build to be minimal. Since all cities will be connected anyway, it does not matter where we start, but assume we start at "a".

a) Assuming we start at city "a" which city would you connect first? Why this city?

- b) What city would you connect next to expand your partial road network?
- c) What would be some characteristics of the resulting "graph" after all the cities are connected?
- d) Does your algorithm come up with the overall best (globally optimal) result?

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2. Prim's algorithm for determining the minimum-spanning tree of a graph is another example of a *greedy algorithm*. Unlike divide-and-conquer and dynamic programming algorithms, greedy algorithms DO NOT divide a problem into smaller subproblems. Instead a greedy algorithm builds a solution by making a sequence of choices that look best ("locally" optimal) at the moment without regard for past or future choices (no backtracking to fix bad choices).

a) What greedy criteria does Prim's algorithm use to select the next vertex and edge to the partial minimum spanning tree?

b) Consider the textbook's Prim's Algorithm code (Listing 7.12 p. 346) which is incorrect.

```
def prim(G, start):
pq = PriorityQueue()
for v in G:
    v.setDistance(sys.maxsize)
    v.setPred(None)
start.setDistance(0)
pq.buildHeap([(v.getDistance(),v) for v in G])
while not pq.isEmpty():
     currentVert = pq.delMin()
     for nextVert in currentVert.getConnections():
       newCost = currentVert.getWeight(nextVert) \
                 + currentVert.getDistance()
       if v in pg and newCost<nextVert.getDistance():
           nextVert.setPred(currentVert)
           nextVert.setDistance(newCost)
           pq.decreaseKey(nextVert, newCost)
```

c) What is wrong with the code? (Fix the above code.)

3. To avoid "massive" changes to the binHeap class, it can store PriorityQueueEntry objects:

```
class PriorityQueueEntry:
 def __init__(self,x,y):
                                                      def __lt__(self, other):
     self.key = x
                                                          return self.key < other.key</pre>
     self.val = y
                                                      def ___gt__(self, other):
 def getKey(self):
                                                          return self.key > other.key
     return self.key
                                                      def ___eq__(self, other):
def getValue(self):
                                                          return self.val == other.val
     return self.val
                                                      def __hash__(self):
 def setValue(self, newValue):
                                                          return self.key
     self.val = newValue
```

- a) Update the above Prim's algorithm code to use PriorityQueueEntry objects.
- b) Why do the __lt__ and __gt__ methods compare key attributes, but __eq__ compare val attributes?

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c) When used for Prim's algorithm what type of objects are the vals compared by __eq_?

- d) What changes to the Graph and Vertex classes need to be made?
- e) Complete the __contains__ and decreaseKey methods.

```
class BinHeap:
def __init_
            (self):
                                                             def ___contains___(self, value):
     self.heapList = [0]
     self.currentSize = 0
def buildHeap(self,alist):
    i = len(alist) // 2
    self.currentSize = len(alist)
     self.heapList = [0] + alist[:]
     while (i > 0):
        self.percDown(i)
         i = i - 1
def percDown(self,i):
     while (i * 2) <= self.currentSize:
        mc = self.minChild(i)
         if self.heapList[i] > self.heapList[mc]:
             tmp = self.heapList[i]
             self.heapList[i] = self.heapList[mc]
             self.heapList[mc] = tmp
                                                              def decreaseKey(self, decreasedValue):
         i = mc
                                                                    """Precondition: decreasedValue
                                                                       in heap already"""
def minChild(self,i):
    if i * 2 + 1 > self.currentSize:
        return i * 2
     else:
        if self.heapList[i*2] < self.heapList[i*2+1]:</pre>
            return i * 2
        else:
            return i * 2 + 1
def percUp(self,i):
     while i / / 2 > 0:
         if self.heapList[i] < self.heapList[i//2]:</pre>
            tmp = self.heapList[i // 2]
            self.heapList[i // 2] = self.heapList[i]
            self.heapList[i] = tmp
         i = i // 2
def insert(self,k):
     self.heapList.append(k)
    self.currentSize = self.currentSize + 1
    self.percUp(self.currentSize)
def delMin(self):
    retval = self.heapList[1]
     self.heapList[1] = self.heapList[self.currentSize]
     self.currentSize = self.currentSize - 1
     self.heapList.pop()
    self.percDown(1)
    return retval
def isEmpty(self):
    return self.currentSize == 0
def size(self):
    return self.currentSize
def __str_(self):
    return str(self.heapList[1:])
```