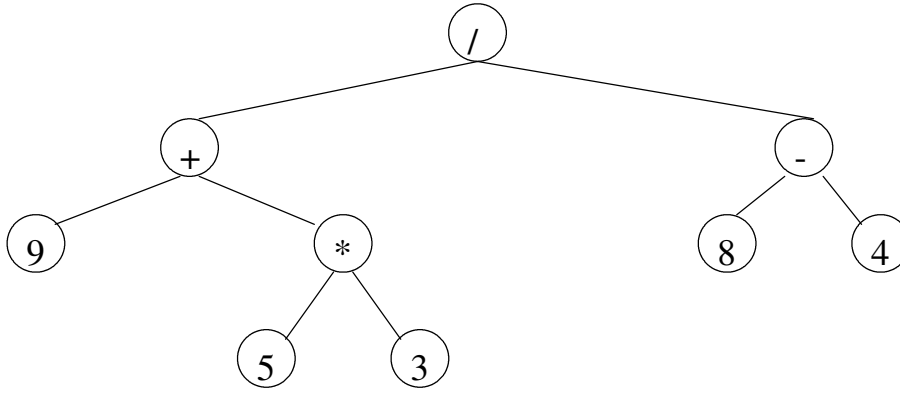


1. Consider the parse tree for $(9 + (5 * 3)) / (8 - 4)$:



a) Identify the following items in the above tree:

- *node* containing “*”
- *edge* from node containing “-” to node containing “8”
- *root* node
- *children* of the node containing “+”
- *parent* of the node containing “3”
- *siblings* of the node containing “*”
- *leaf* nodes of the tree
- *subtree* whose root is node contains “+”
- *path* from node containing “+” to node containing “5”
- *branch* from root node to “3”

b) Mark the *levels* of the tree (level is the number of edges on the path from the root)

c) What is the *height* (max. level) of the tree?

2. In Python an easy way to implement a tree is as a list of lists where a tree look like:

[“node value”, remaining items are subtrees for the node each implemented as a list of lists]

Complete the list-of-lists representation look like for the above parse tree:

['/', ['+', _____], ['-', _____]]

3. Consider a “linked” representations of a BinaryTree. For the expression $((4 + 5) * 7)$, the binary tree would be:

```

class BinaryTree:
    def __init__(self, rootObj):
        self.key = rootObj
        self.leftChild = None
        self.rightChild = None
    
```

```

graph TD
    Root["key: '*'  
leftChild: '+'  
rightChild: '7'"]
    Plus["key: '+'  
leftChild: '4'  
rightChild: '5'"]
    Seven["key: '7'"]
    Four["key: '4'"]
    Five["key: '5'"]

    Root --> Plus
    Root --> Seven
    Plus --> Four
    Plus --> Five
    
```

```

import operator
class BinaryTree:
    def __init__(self, rootObj):
        self.key = rootObj
        self.leftChild = None
        self.rightChild = None

    def insertLeft(self, newNode):
        if self.leftChild == None:
            self.leftChild = BinaryTree(newNode)
        else:
            t = BinaryTree(newNode)
            t.left = self.leftChild
            self.leftChild = t

    def insertRight(self, newNode):
        if self.rightChild == None:
            self.rightChild = BinaryTree(newNode)
        else:
            t = BinaryTree(newNode)
            t.right = self.rightChild
            self.rightChild = t

    def isLeaf(self):
        return ((not self.leftChild) and
                (not self.rightChild))

    def getRightChild(self):
        return self.rightChild

    def getLeftChild(self):
        return self.leftChild

    def setRootVal(self, obj):
        self.key = obj

    def getRootVal(self,):
        return self.key

    def inorder(self):
        if self.leftChild:
            self.leftChild.inorder()
        print(self.key)
        if self.rightChild:
            self.rightChild.inorder()

    def postorder(self):
        if self.leftChild:
            self.leftChild.postorder()
        if self.rightChild:
            self.rightChild.postorder()
        print(self.key)

```

a) Fix the insertLeft and insertRight code:
 (Listing 6.6 and 6.7 are wrong in the text on pp. 242-3)

```

def preorder(self):
    print(self.key)
    if self.leftChild:
        self.leftChild.preorder()
    if self.rightChild:
        self.rightChild.preorder()

def printexp(self):
    if self.leftChild:
        print('(', end=' ')
        self.leftChild.printexp()
    print(self.key, end=' ')
    if self.rightChild:
        self.rightChild.printexp()
    print(')', end=' ')

def postordereval(self):
    ops = {'+':operator.add, '-':operator.sub,
          '*':operator.mul, '/':operator.truediv}
    res1 = None
    res2 = None
    if self.leftChild:
        res1 = self.leftChild.postordereval()
    if self.rightChild:
        res2 = self.rightChild.postordereval()
    if res1 and res2:
        return ops[self.key](res1, res2)
    else:
        return self.key

```

Some corresponding external (non-class) functions:

```

def inorder(tree):
    if tree != None:
        inorder(tree.getLeftChild())
        print(tree.getRootVal())
        inorder(tree.getRightChild())

def printexp(tree):
    if tree.leftChild:
        print('(', end=' ')
        printexp(tree.getLeftChild())
    print(tree.getRootVal(), end=' ')
    if tree.rightChild:
        printexp(tree.getRightChild())
    print(')', end=' ')

def height(tree):
    if tree == None:
        return -1
    else:
        return 1 +
            max(height(tree.leftChild),
                height(tree.rightChild))

```

```

def printexp(tree):
    sVal = ""
    if tree:
        sVal = '(' + printexp(tree.getLeftChild())
        sVal = sVal + str(tree.getRootVal())
        sVal = sVal + printexp(tree.getRightChild()) + ')'
    return sVal

def postordereval(tree):
    ops = {'+':operator.add, '-':operator.sub,
          '*':operator.mul, '/':operator.truediv}
    res1 = None
    res2 = None
    if tree:
        res1 = postordereval(tree.getLeftChild())
        res2 = postordereval(tree.getRightChild())
        if res1 and res2:
            return ops[tree.getRootVal()](res1, res2)
    else:
        return tree.getRootVal()

```

b) If `myTree` is the `BinaryTree` object for the expression: $((4 + 5) * 7)$, what gets printed by a call to:

<code>myTree.inorder()</code>	<code>myTree.preorder()</code>	<code>myTree.postorder()</code>	<code>inorder(myTree)</code>

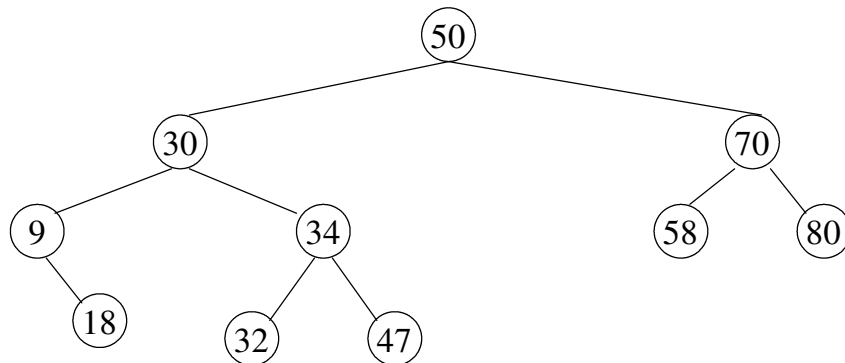
c) If `myTree` is the `BinaryTree` object for the expression: $((4 + 5) * 7)$, what gets printed by a call to `myTree.printexp()`?

d) If `myTree` is the `BinaryTree` object for the expression: $((4 + 5) * 7)$, what gets printed by a call to `myTree.postordereval()`?

e) From an class/Abstract Data Type (ADT) point of view, why are the external versions of the methods “better”?

f) Write the `height` method for the `BinaryTree` class.

4. Consider the Binary Search Tree (BST). For each node, all values in the left-subtree are $<$ the node and all values in the right-subtree are $>$ the node.



- Starting at the root, how would you find the node containing “32”?
- Starting at the root, when would you discover that “65” is not in the BST?
- Starting at the root, where would be the “easiest” place to add “65”?
- Where would we add “5” and “33”?