3. Complete the recursive strHelper function in the str method for our OrderedList class.

def_str_(self):

""" Returns a string representation of the list with a space between each item. """

def strHelper(current):

if correct = None e

lill

leftorm

else;

return str (current, qcf Data()) + "(tail)"

return "(head) " + strHelper(self._head) + "(tail)"

4. Some mathematical concepts are defining by recursive definitions. One example is the Fibonacci series: 0, 1(1)2, 3, 5, 8, 13, 21, 34, 55, \$\frac{1}{3}\$

After the second number, each number in the series is the sum of the two previous numbers. The Fibonacci series can be defined recursively as:

 $\begin{aligned} &Fib_0 = 0\\ &Fib_1 = 1\\ &Fib_N = Fib_{N-1} + Fib_{N-2} \text{ for } N \geq 2. \end{aligned}$

a) Complete the recursive function:

def fib (n):

if N== 0: return 0 elif n== 10 return 1 else.

b) Draw the *call tree* for fib(5)

3). 3 9 p. 76 (3) c

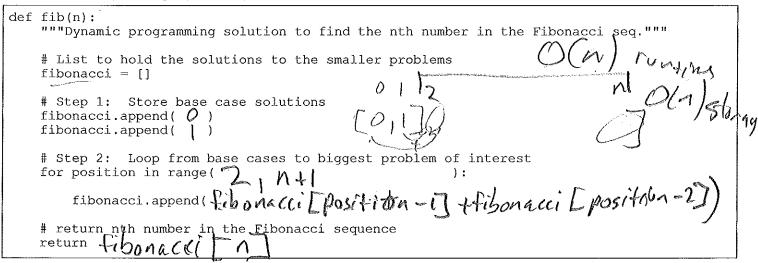
b(i) fib(i) fib(o)

fiblic fibli)

mylist Orderedlist mar of 21 str (my list) call from main: Stattelpers retially. YKE return" +o (***) Current None Stellelou return "me" to(xxx) Lurrent strtlelpk (XXX) vet addi strtlelpe. Correct return "CUMU" to (YXX) retally (* X) call-franc Current return "ay cum" to (4x) retially str call self) Neturn "(head) a complail"
to (*) Mah's myList Call frame

Data Structures (CS 1520)	Lecture 9	Name:_	
c) On my office computer, the call to fib(40) take fib(42) takes 56 seconds. How long would you e		9/sec	Fib(43)
d) How long would you guess calculating fib(10	0) would take on my o	ffice computer? 57	sec/ 35,500
e) Why do you suppose this recursive fib function redundant calculate	ot years n is so slow?	1. 35 Aib	42) +/h(41)
reachant calculat	(00) 01 110		1 1/2/1
2 ⁿ =	-2×17	Andry	171240
f) What is the computational complexity?	2/2) 15/1		
g) How might we speed up the calculation of the	Fibonacci series?		the first transfer of the second seco
use dyn. p	vogramming	A A	
5. A VERY POWERFUL concept in Computer Stellminate the redundancy of divide-and-conquer a storing their answers, and looking up their answers.	algorithms by calculati	ng the solutions to sm	aller problems first,
We can use a list to store the answers to smaller p To transform from the recursive view of the probl steps:		-	ou can do the following

- 1) Store the solution to smallest problems (i.e., the base cases) in a list
- 2) Loop (no recursion) from the base cases up to the biggest problem of interest. On each iteration of the loop we:
 - solve the next bigger problem by looking up the solution to previously solved smaller problem(s)
 - store the solution to this next bigger problem for later usage so we never have to recalculate it
- a) Complete the dynamic programming code:



Running the above code to calculate fib(100) would only take a fraction of a second.

b) One tradeoff of simple dynamic programming implementations is that they can require more memory since we store solutions to all smaller problems. Often, we can reduce the amount of storage needed if the next larger problem (and all the larger problems) don't really need the solution to the really small problems, but just the larger of the smaller problems. In fibonacci when calculating the next value in the sequence how many of the previous solutions are use three variables a b of O(1) storage of both O(h) exec needed? 2

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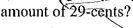
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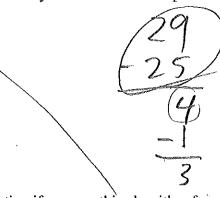
Lecture 10

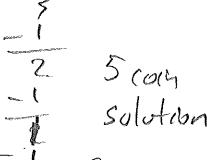
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1. Consider the coin-change problem: Given a set of coin types and an amount of change to be returned, determine the fewest number of coins for this amount of change.

a) What greedy algorithm would you use to solve this problem with US coin types of {1, 5, 10, 25, 50} and a change







b) Do you get the correct solution if you use this algorithm for coin types of [4, 5, 10,12,25, 50] and a change amount of 29-cents?

3 con soldion production possible 12+12+5

2. One way to solve this problem in general is to use a divide-and-conquer algorithm. Recall the idea of

Divide-and-Conquer algorithms.

Solve a problem by:

• dividing it into smaller problem(s) of the same kind

• solving the smaller problem(s) recursively

• use the solution(s) to the smaller problem(s) to solve the original problem

294 change

[1,5,10,12,25,50]

a) For the coin-change problem, what determines the size of the problem?

and

(oin Set: [1,5,12,25,50]

Size

b) How could we divide the coin-change problem for 29-cents into smaller problems?

reduce amount of change

c) If we knew the solution to these smaller problems, how would be able to solve the original problem?

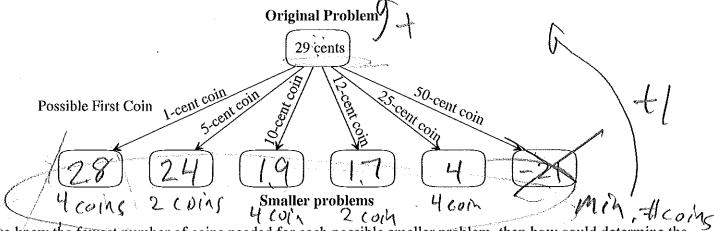
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3. After we give back the first coin, which smaller amounts of change do we have?



4. If we knew the fewest number of coins needed for each possible smaller problem, then how could determine the fewest number of coins needed for the original problem?

5. Complete a recursive relationship for the fewest number of coins.

FewestCoins(change) =
$$\begin{cases} \min(\text{FewestCoins}(change - coin)) + | & \text{if change} \notin \text{CoinSet and coin} \leq \text{change} \\ \hline 1 & \text{if change} \notin \text{CoinSet and coin} \leq \text{change} \end{cases}$$

6. Complete a couple levels of the recursion tree for 29-cents change using the set of coins {1, 5, 10, 12, 25, 50}.

