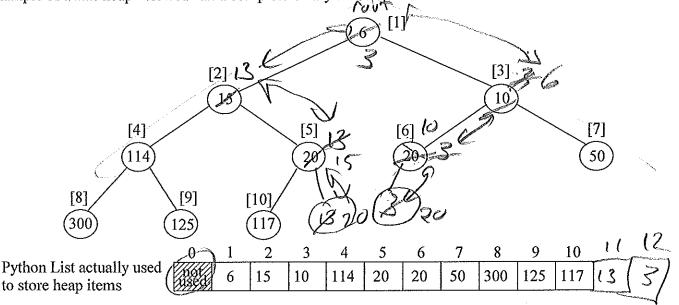
Data Structures (CS	<b>S</b> 134	¿()
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Lecture 7

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1. Section 6.6 discusses a very "non-intuitive", but powerful list/array-based approach to implement a priority queue, call a binary heap. The list/array is used to store a complete binary tree (a full tree with any additional leaves as far left as possible) with the items being arranges by heap-order property, i.e., each node is  $\leq$  either of its children. An example of a min heap "viewed" an a complete binary tree would be:

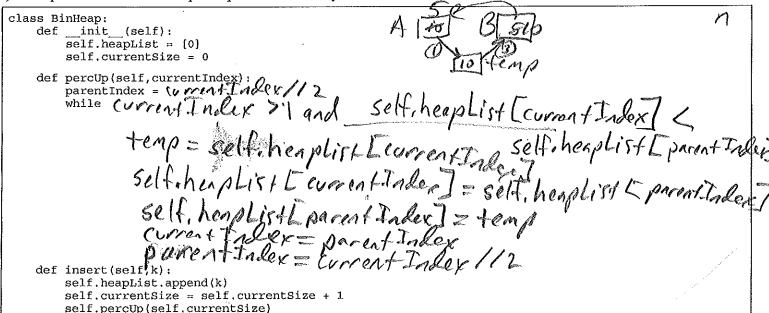


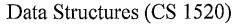
- a) For the above heap, the list/array indexes are indicated in [ ]'s. For a node at index i, what is the index of:
- its left child if it exists:
- its right child if it exists: 2 x 1
- its parent if it exists:
- b) What would the above heap look like after inserting 13 and then 3? (show the changes on above tree)

General Idea of insert(newItem):

- append newItem to the end of the list (easy to do, but violates heap-order property)
- restore the heap-order property by repeatedly swapping the newItem with its parent until it percolates to correct spot
- c) What is the big-oh notation for inserting a new item in the heap? O(log 2n)

d) Complete the code for the percUp method used by insert.

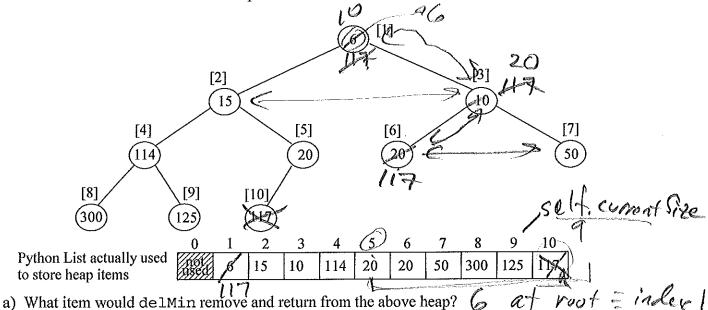




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2. Now let us consider the delMin operation that removes and returns the minimum item.



- b) What is the quickest way to fill the hole left by delMin?
- c) What new problem does this cause?

General Idea of delMin():

- remember the minimum value so it can be returned later (easy to find at index 1)
- copy the last item in the list to the root, delete it from the right end, decrement size
- restore the heap-order property by repeatedly swapping this item with its smallest child until it *percolates down* to the correct spot
- return the minimum value
- d) What would the above heap look like after delMin? (show the changes on above tree)
- e) Complete the code for the percDown method used by delMin.

def percDown(self, currentIndex): class BinHeap: while current tablex x2 <= self-cumasize: def minchild (self, i): E returns index of minchild if i \* 2 + 1 > self.currentSize: # if only left child
 return i \* 2 min Child Index = self, min Child else: if self.heapList[i \* 2] < self.heapList[i \* 2 + 1]:</pre> (curren Frdex) return i \* 2 else: return i \* 2 + 1 if self-heaplist [commatinals def delMin(self): retval = self.heapList[1] > self horpLirt Emin Child Index +emp = self heapLirt Exurrent To self.heapList[1] = self.heapList[self.currentSize] self.currentSize = self.currentSize - 1 self.heapList.pop() self.percDown(1) self. heaplist correct Tale return retval = Self. hogoLill TrainChild Tabil Self, herskitt Timin Chill Taker 1

f) What is the big-oh notation for delMin?  $O(log_{iN})$ 

Coment Index = min Chillenter Lecture 7 - Page 2

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Once we have a working BinHeap, then implementing the PriorityQueue class using a BinHeap is a piece of cake:

```
### File: priority_queue.py
from binheap import BinHeap

class PriorityQueue:
    def __init__(self):
        self._heap = BinHeap()

def isEmpty(self):
        return self._heap.isEmpty()

def enqueue(self, item):
        self._heap.insert(item)

def dequeue(self):
        return self._heap.delMin()

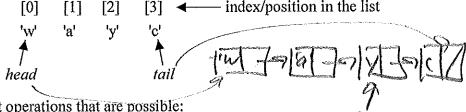
def size(self):
        return self._heap.size()

def __str__(self):
        return str(self._heap)
```

```
>>> q = PriorityQueue()
>>> print(q)
[]
>>> q.enqueue(5)
>>> q.enqueue(1)
>>> q.enqueue(7)
>>> print(q)
[1, 5, 7]
>>> q.dequeue()
1
>>> print(q)
[5, 7]
```

3. A "list" is a generic term for a sequence of items in a linear arrangement. Unlike stacks, queues and deques access to list items is not limited to either end, but can be from any position in the list. The general terminology of a list is illustrated by:

"Abstract view of a list"



There are three broad categories of list operations that are possible:

- index-based operations the list is manipulated by specifying an index location, e.g., myList.insert(3, item) # insert item at index 3 in myList
- content-based operations the list is manipulated by specifying some content (i.e., item value), e.g., myList.remove(item) # removes the item from the list based on its value
- cursor-base operations a *cursor* (current position) can be moved around the list, and it is used to identify list items to be manipulated, e.g.,

myList.first() # sets the cursor to the head item of the list

myList.next() # moves the cursor one position toward the tail of the list

myList.remove() # deletes the second item in the list because that's where the cursor is currently located

The following table summarizes the operations from the three basic categories on a list, L:

<b>Index-based operations</b>	Content-based operations	cursor-based operations
L.insert(index, item)	L.add(item)	L.hasNext()
item = L[index]	L.remove(item)	L.next()
L[index] = newValue	L.search(item) #return Boolean	L.hasPrevious()
L.pop(index)	i = L.index(item)	L.previous()
		L.first()
		L.last()
		L.insert(item)
		L.replace(item)
		L.remove()

Built-in Python lists are unordered with a mixture of index-based and content-based operations. We know they are implemented using a contiguous block of memory (i.e., an array). The textbook talks about an unordered list ADT, and a sorted list ADT which is more content-based. Both are implemented using a singly-linked list.

a) Why would a singly-linked list be a bad choice for implementing a cursor-based list ADT?

which singly-linked Notes but O(1) with doubly-linked Note2 Way Lecture 7 - Page 3