

Question 3. (15 points) Consider the following simple sorts discussed in class -- all of which sort in ascending order.

```
def bubbleSort(myList):
    for lastUnsortedIndex in range(len(myList)-1, 0, -1):
        for testIndex in range(lastUnsortedIndex):
            if myList[testIndex] > myList[testIndex+1]:
                temp = myList[testIndex]
                myList[testIndex] = myList[testIndex+1]
                myList[testIndex+1] = temp
```

```
def insertionSort(myList):
    for firstUnsortedIndex in range(1, len(myList)):
        itemToInsert = myList[firstUnsortedIndex]
        testIndex = firstUnsortedIndex - 1
        while testIndex >= 0 and myList[testIndex] > itemToInsert:
            myList[testIndex+1] = myList[testIndex]
            testIndex = testIndex - 1

        myList[testIndex + 1] = itemToInsert
```

```
def selectionSort(aList):
    for lastUnsortedIndex in range(len(aList)-1, 0, -1):
        maxIndex = 0
        for testIndex in range(1, lastUnsortedIndex+1):
            if aList[testIndex] > aList[maxIndex]:
                maxIndex = testIndex
        # exchange the items at maxIndex and lastUnsortedIndex
        temp = aList[lastUnsortedIndex]
        aList[lastUnsortedIndex] = aList[maxIndex]
        aList[maxIndex] = temp
```

Timings of Above Sorting Algorithms on 10,000 items (seconds)

| Type of sorting algorithm | Initial Ordering of Items | | |
|---------------------------|---------------------------|-----------|--------------|
| | Descending | Ascending | Random order |
| bubbleSort.py | 23.3 | 7.7 | 15.8 |
| insertionSort.py | 14.2 | 0.004 | 7.3 |
| selectionSort.py | 7.3 | 7.7 | 6.8 |

a) Explain why bubbleSort on a descending list (23.3 s) takes longer than bubbleSort on an ascending list (7.7 s).

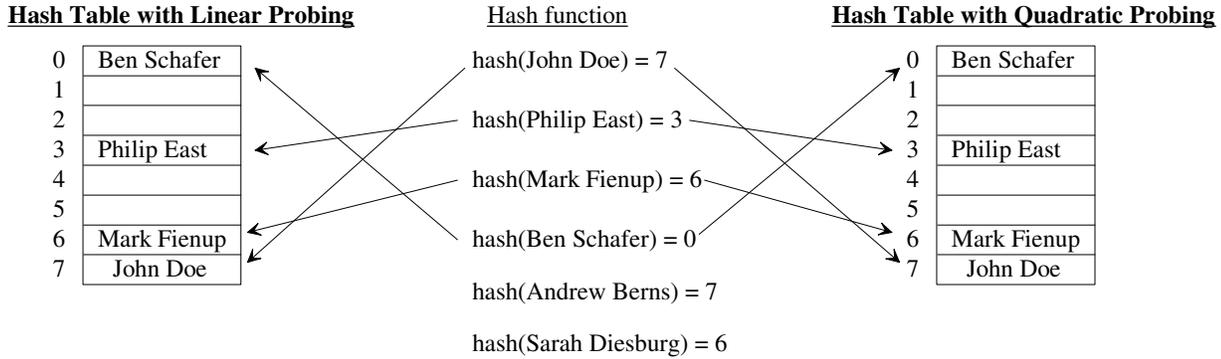
b) Explain why bubbleSort on a descending list (23.3 s) takes longer than insertionSort on a descending list (14.2 s).

c) Explain why selectionSort is $O(n^2)$ in the worst-case.

Question 4. Two common rehashing strategies for open-address hashing are linear probing and quadratic probing:

| | |
|-------------------|---|
| quadratic probing | Check the square of the attempt-number away for an available slot, i.e., $[\text{home address} + ((\text{rehash attempt \#})^2 + (\text{rehash attempt \#})) // 2] \% (\text{hash table size})$, where the hash table size is a power of 2. Integer division is used above |
|-------------------|---|

a) (8 points) Insert “Andrew Berns” **and then** “Sarah Diesburg” using Linear (on left) and Quadratic (on right) probing.



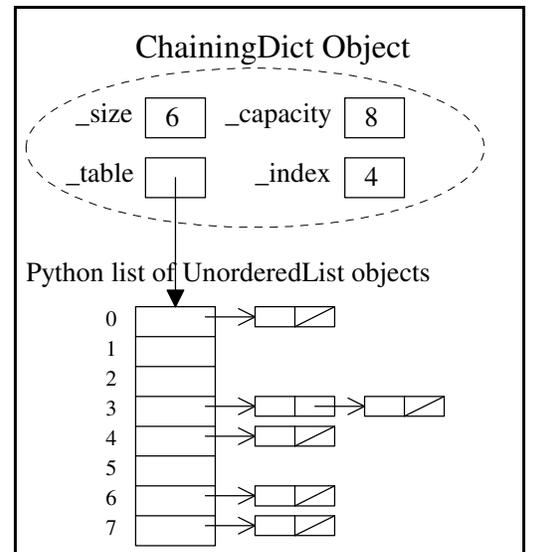
b) In open-address hashing (like the pictures above), the average number probes/compares for various load factors is:

| Probing Type | Search outcome | Load Factor, λ | | | | |
|-------------------|----------------|------------------------|------|------|-------|---------|
| | | 0.25 | 0.5 | 0.67 | 0.8 | 0.99 |
| Linear Probing | unsuccessful | 1.39 | 2.50 | 5.09 | 13.00 | 5000.50 |
| | successful | 1.17 | 1.50 | 2.02 | 3.00 | 50.50 |
| Quadratic Probing | unsuccessful | 1.37 | 2.19 | 3.47 | 5.81 | 103.62 |
| | successful | 1.16 | 1.44 | 1.77 | 2.21 | 5.11 |

The "general rule of thumb" tries to keep the load factor (i.e., # items / hash-table size) between 0.5 and 0.67.

- (4 points) Why don't you want the load factor to exceed 0.67?
- (3 points) Why don't you want the load factor to be less than 0.5?

c) (5 points) In closed-address hashing (e.g., ChainingDict picture to the right) if the load factor (# items / hash table size) is 10, what would you expect for the average number of probes/compares of a successful search? (Justify your answer)



Question 5. (20 points) In class we discussed the bubbleSort code shown in question 3 on page 2 which sorts in ascending order (smallest to largest) and builds the sorted part on the right-hand side of the list.

For this question write a variation of bubble sort that:

- sorts in **descending order** (largest to smallest), and
- builds the **sorted part on the left-hand side** of the list, i.e.,



Inner loop scans from right to left across the unsorted part swapping adjacent items that are "out of order"

```
def bubbleSortVariation(myList):
```

Question 6. Recall the general idea of Quick sort:

- Partition by selecting a pivot item at "random" and then rearrange (*partitioning*) the unsorted items such that::
- Quick sort the unsorted part to the left of the pivot
- Quick sort the unsorted part to the right of the pivot

| Pivot Index | | |
|----------------------|------------|-----------------------|
| All items < to Pivot | Pivot Item | All items >= to Pivot |

a) (5 points) Explain why quick sort is $O(n \log_2 n)$ when sorting initially randomly ordered items. (n is the $\text{len}(\text{myList})$)

b) (5 points) Explain why quick sort is $O(n^2)$ is the worst-case. (n is the $\text{len}(\text{myList})$)