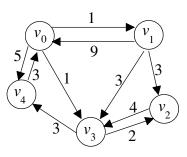
Lecture 25

Name:

1. Consider the following directed graph (diagraph) G = (V, E):



a) What is the set of vertices? V =

b) An edge can be represented by a tuple (from vertex, to vertex [, weight]). What is the set of edges?

E =

c) A path is a sequence of vertices that are connected by edges. In the graph G above, list two different pathes from v_0 to v_3 .

d) A cycle in a directed graph is a path that starts and ends at the same vertex. Find a cycle in the above graph.

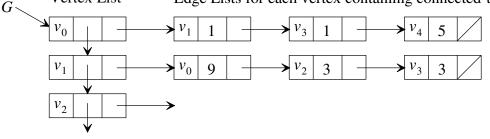
2. Like most data structures, a graph can be represented using an array, or as a linked list of nodes. The array representation is a two-dimensional array (called an *adjacency matrix*) whose elements contain information about the edges and the vertices corresponding to the indices. (Python could use a list-of-lists)

a) Complete the following adjacency matrix for the above graph. (Here a missing edge is represented by ∞ .) (to vertex)

		\mathcal{V}_0	v_1	v_2	v_3	\mathcal{V}_4
(from vertex)	v_0	0	1	∞	1	5
	v_1	9	0	3	3	∞
	v_2					
	v_3					
	\mathcal{V}_4					

b) The linked representation maintains a linked-list (or Python dictionary) of vertices with each vertex maintaining a linked list of other vertices that it connects to. Complete the adjacency list representation below:

Vertex List Edge Lists for each vertex containing connected-to and edge-weight information



Data Structures (CS 1520)

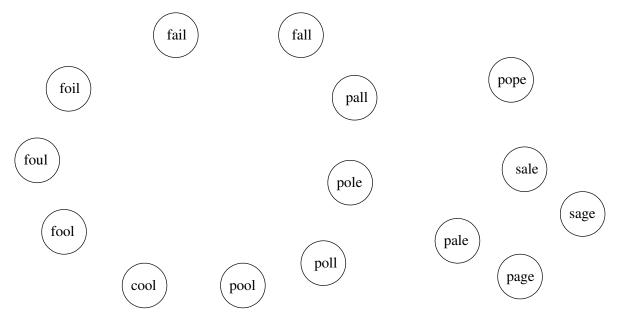
Lecture 25

Name:__

3. Graphs can be used to solve many problems by modeling the problem as a graph and using "known" graph algorithm(s). For example, consider the *word-ladder puzzle* where you tranform one word into another by changing one letter at a time, e.g., transform FOOL into SAGE by FOOL \rightarrow FOIL \rightarrow FAIL \rightarrow FAIL \rightarrow PALL \rightarrow PALE \rightarrow SALE \rightarrow SAGE.

We can use a graph algorithm to solve this problem by constructing a graph such that

- a word represents a vertex
- an edge represents?
- a word ladder transformation from one word to another represents?
- 4. For the words listed below, draw the graph of question 3



- a) List a different transformation from FOOL to SAGE
- b) If we wanted to find the shortest transformation from FOOL to SAGE, what does that represent in the graph?
- c) There are two general approaches for traversing a graph from some starting vertex *s*:
- Breadth First Search (BFS) where you find all vertices a distance 1 (directly connected) from s, before finding all vertices a distance 2 from s, etc.
- Depth First Search (DFS) where you explore as deeply into the graph as possible. If you reach a "dead end," we backtrack to the deepest vertex that allows us to try a different path.

Which of these traversals would be helpful for finding the **shortest** solution to the word-ladder puzzle?