

A property is **static** when its value can be determined by looking at the text of a program.

A property is **dynamic** when the program must be executed in order to determine its value.

We can use static properties of a program to detect errors and to improve program performance at interpretation or compile time.

.

## Racket--

$\langle \text{exp} \rangle ::= \langle \text{varref} \rangle$   
          |  $(\text{lambda } (\langle \text{var} \rangle) \langle \text{exp} \rangle)$   
          |  $(\langle \text{exp} \rangle \langle \text{exp} \rangle)$

.

A variable reference **is bound** or **occurs bound** in an expression if it refers to the formal parameter in the expression.

A variable reference **is free** or **occurs free** in an expression if it is not bound.

.

```
int sumOfSquares( int m, int n )  
{  
    return m*m + n*n;  
}
```

```
int weightedSum( int m, int n )  
{  
    return scale*m + scale*n;  
}
```

•

Free and bound variables in the Racket--:

```
(lambda (z) x)
```

```
(lambda (x) x)
```

```
((lambda (x) x) y)
```

```
(lambda (y)
```

```
  ((lambda (x) x) y) )
```

```
(lambda (f)
```

```
  (lambda (x)
```

```
    (lambda (y)
```

```
      (+ (f x) (f y))))))
```

.

Today, we use our recursive techniques  
to write a program that  
**processes programs**  
in Racket--.

Our task is straightforward:

**Does a variable occur bound  
in a given piece of code?**

.

A variable  $v$  **occurs bound** in an expression  $exp$  if and only if:

- $exp$  is of the form  $(\lambda (var) body)$  and either
  - $v$  occurs bound in  $body$ , or
  - $v$  occurs free in  $body$  and  $v$  is the same as  $var$ .
- $exp$  is of the form  $(exp1\ exp2)$  and  $v$  occurs bound in either  $exp1$  or  $exp2$ .

By definition, no variable occurs bound in a variable reference.

.

A variable  $v$  **occurs free** in an expression  $exp$  if and only if:

- $exp$  is a variable reference and is the same as  $v$
- $exp$  is of the form  $(exp1\ exp2)$  and  $v$  occurs free in either  $exp1$  or  $exp2$ .
- $exp$  is of the form  $(\lambda(var)\ body)$ ,  $v$  is different from  $var$ , and  $v$  occurs free in  $body$ .

•



## **syntax procedures**

pair

-----

list

-----

**type predicate**

pair?

list?

**access procedures**

car

cdr

first

rest

**constructor**

cons

list

.